

# Industrial Organization - V

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## Next class

- ▶ Entry and exit
- ▶ Review of class material
- ▶ 2 minutes presentations on your case studies + feedback from your colleagues.

### Rules for the 2 mins presentations

- ▶ Each group selects a presenter.
- ▶ The presenter introduces the case, and motivates the choice.
- ▶ The presenter briefly mentions the major points of interest.
- ▶ A quick discussion with the class follows.

# Today's class

- ▶ Closing words on auctions
- ▶ Geographic competition: Hotelling model

# Auctions

Different ways of determining the pricing.

Who sets the price:

- ▶ Firm: pricing
- ▶ Buyer: auctions
- ▶ Both: negotiations

## Auctions

Among the best forms of price-discrimination by self selection.

The *bidders* want to maximize profits, similarly to the rule of  $MR = MC$  for firms.

# Most popular forms of auctions

- ▶ Ascending price auctions (English auction)
- ▶ Second price sealed bid
- ▶ First price sealed bid
- ▶ First price descending auction

## First price private value auction

Participants write secretly in an envelope their bid. The highest bid wins and the buyer pays the price of their bid.

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## Optimal strategy

In the first price sealed bid auction, the best bid is given by:

$$b(v) = \frac{(N-1)}{N}v$$

## Descending price auctions

In terms of strategies, first price sealed bid auctions are equivalent to descending price auction.

**Buyers bid less than their valuation.**

## Second price sealed bid auction

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### Ascending price auctions

In terms of strategies, second price sealed bid auctions are equivalent to ascending price auction.

**Buyers bid exactly an amount equal to their valuation.**

# Explanations to over-bidding

## Explanation 1

**Risk aversion:** the tendency to prefer outcomes with low uncertainty to those with high uncertainty.

## Explanation 2

**Underestimation of winning probability:** if you systematically think that the others have higher valuations, and so you underestimate your probability of winning.

# Winner's curse

It occurs if a bidder does not realize that winning the auction implies that the others' valuations were low.

The winner's curse occurs in common value options: the value of the good is objective, but buyers only have access to partial information about the good quality.

The key point is that winning the auction is bad news about the value of the item for the winner. It means that he or she was the most optimistic and, if bidders are correct in their estimations on average, that too much was paid.

# Geographic differentiation

In 1929, Hotelling developed a model ahead of his time.

A location game

- ▶ Consumers are *uniformly* distributed on a segment (10km).
- ▶ **Two** sellers, each located at the end of the segment (**location is fixed**).
- ▶ Sellers simultaneously set prices as in Bertrand.

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- ▶ **Two** sellers, each located at the end of the segment (**location is fixed**).
- ▶ Sellers simultaneously set prices as in Bertrand.
- ▶ A consumer located at the point  $x$  must travel a distance  $x$  to reach the first seller.
- ▶ The same consumer travels a distance  $(1 - x)$  to reach the second seller.
- ▶ There is a travel cost  $t$ .

# The model

From the perspective of the consumer located at  $x$ :

## Cost of buying

- ▶ From firm 1:  $p'_1 = p_1 + tx \rightarrow$  the actual price of the good plus transportation costs (that depend on the distance).
- ▶ From firm 2:  $p'_2 = p_2 + t(1 - x)$ .

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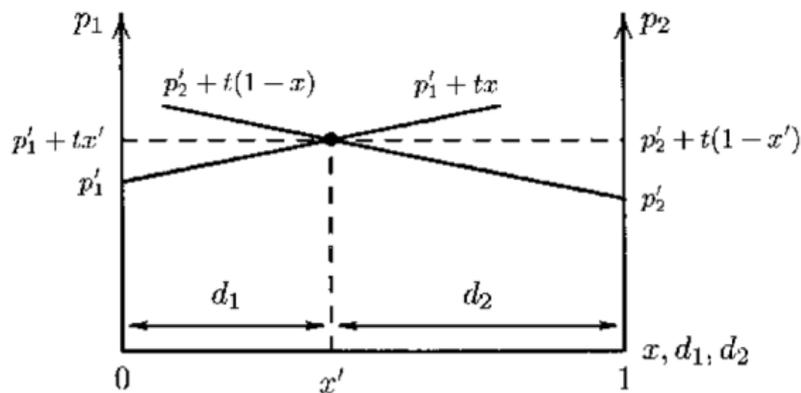


FIGURE 12.1 HOTELLING MODEL: TOTAL CONSUMER COST.

## Demand curves

We consider different prices, and that all consumers buy.  
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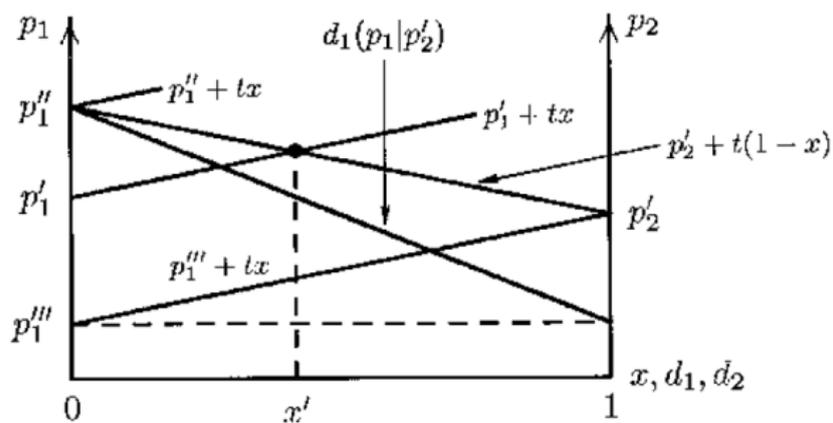


FIGURE 12.2 HOTELLING MODEL: FIRM 1'S DEMAND.

# Equilibrium

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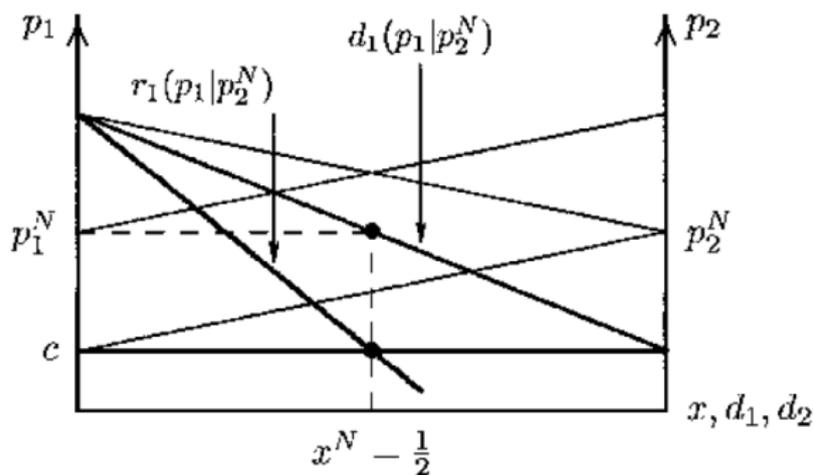


FIGURE 12.3 HOTELLING MODEL: EQUILIBRIUM.

# What did we learn?

We can interpret  $t$  as the degree of differentiation. Why?

Hotelling as product differentiation

Instead of space we measure distance in characteristics. The higher the transportation cost  $t$  implies that the consumers perceive as more costly to get a characteristic different from their preferred one.

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Product differentiation and market power

The greater the degree of product differentiation, the greater the market power  $\implies$  POSITIVE MARGINS.

# Back to Bertrand

The Bertrand model requires the following assumptions:

- ▶ No capacity constraints
- ▶ One-shot interactions
- ▶ Homogeneous product

The Bertrand paradox

Even with two firms only, if the conditions above hold, firms make zero profits like in perfect competition.

# Solving the paradox

It is clear that in reality firms operating in duopolies (and more generally in oligopolies) make positive profits.

The cases we studied

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- ▶ ~~One-shot interactions~~  $\implies$  Collusion (prices are higher than  $MR$ , price wars may occur).
- ▶ ~~Homogeneous product~~  $\implies$  Hotelling with fixed “locations” (Firms share the market, prices depend on the degree of differentiation).

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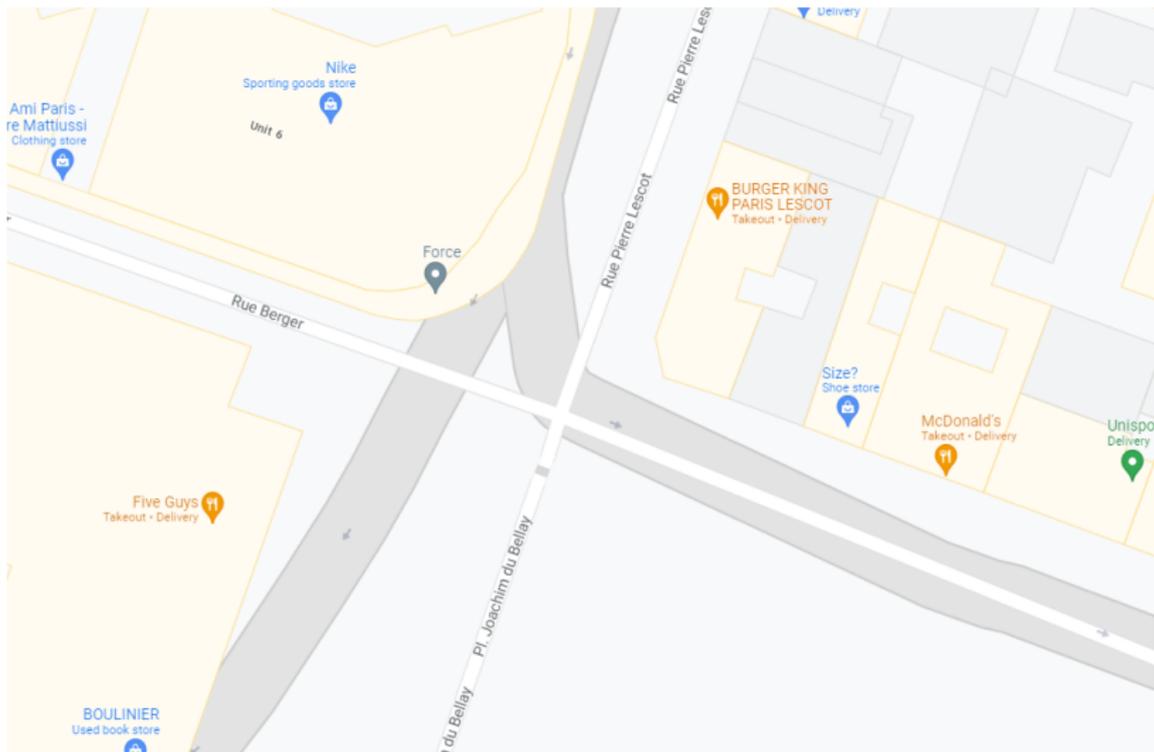
Equilibrium with  $n$  firms ( $n$  even)

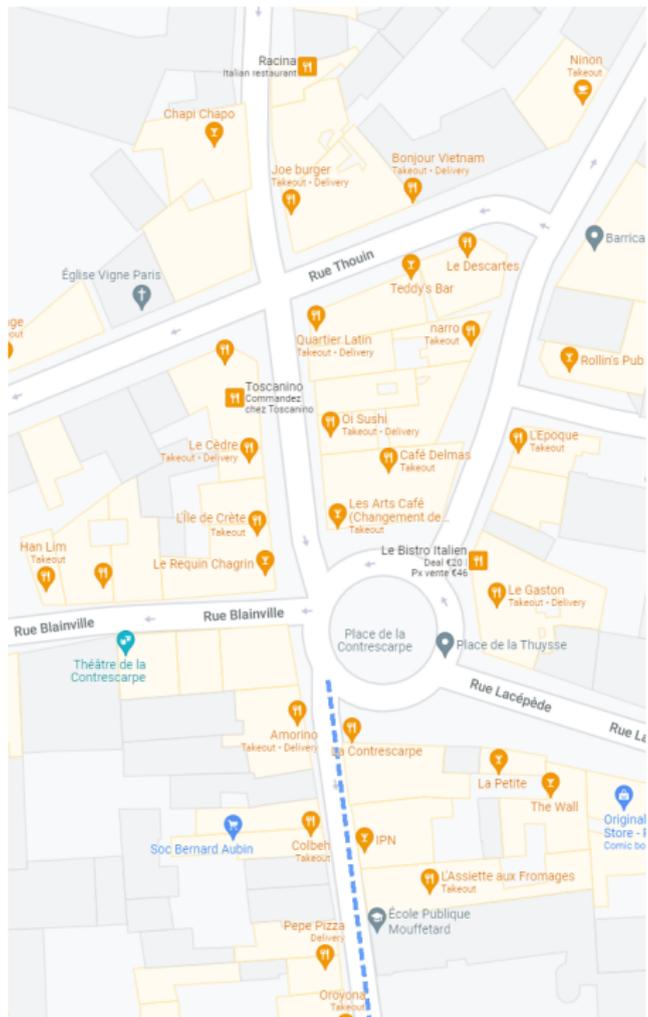
Exactly two firms will be at these points:  $[1/n, 3/n, \dots, (n-1)/n]$

Does it work?









## Proof of the result

Each position attracts  $2/n$  customers, which are indifferent from buying from either firm.



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Case 1: going to other firms' location

It is easy to check that it is not profitable: It is easy to see that deviating, the firm now gets  $2/3n < 1/n$ .

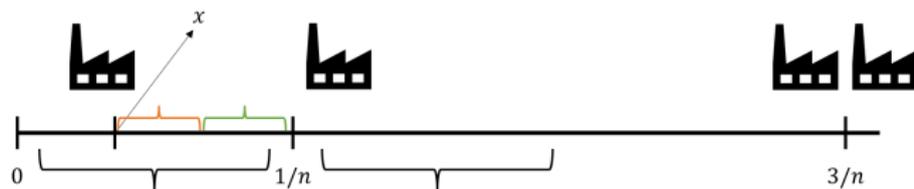
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Case 2: going closer to the extremes



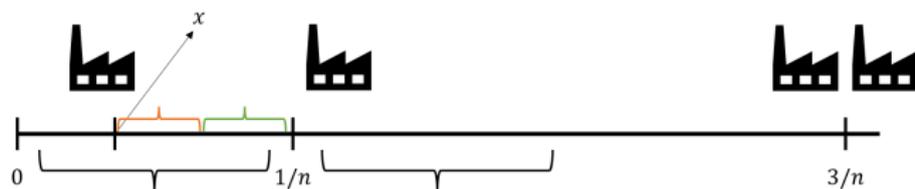
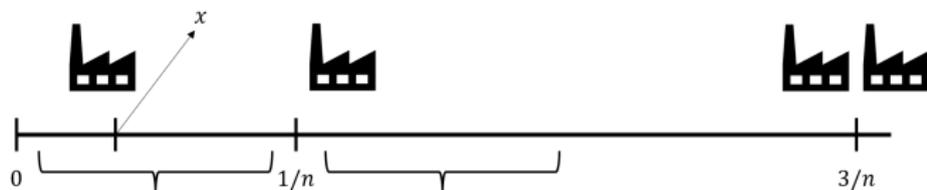
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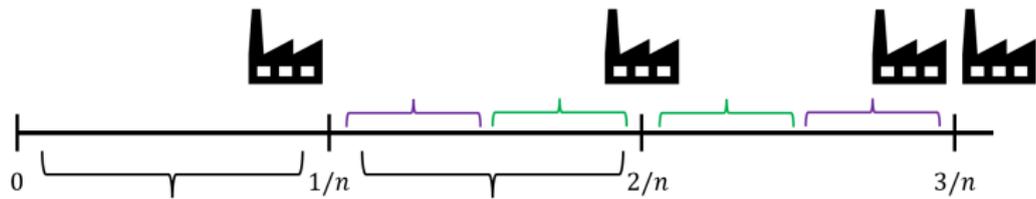
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This deviation yields clearly less profits.

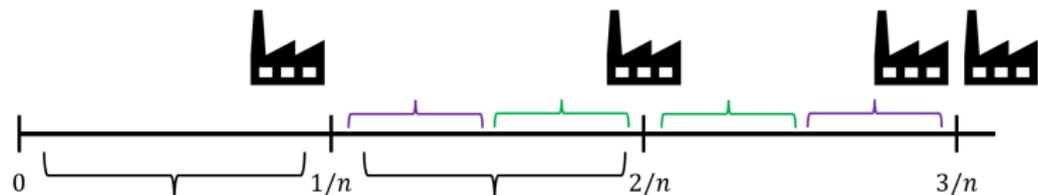
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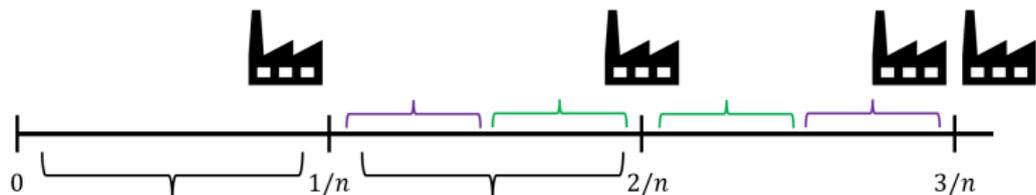
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By deviating, the firm gets exactly  $1/n$  customers, like the firm did in the original position. The profits are exactly the same, so it is not profitable.

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## Conclusion

We considered all possible deviations, none of which is profitable. Therefore the initial configuration is an equilibrium.  $\square$

Merci pour votre attention